

NASH EQUILIBRIUM: THEORY

PREFERENCES

- **Ordinal preferences** compare items, but not the intensity of preferences.
 - For example, I like bananas more than apples.
- **Cardinal preferences** compare items, but, also, the intensity of preferences.
 - For example, I like bananas 2.5 times more than apples.
- However, cardinal preferences require more assumptions.
- For now (i.e. chapters 2-3), we will assume preferences are ordinal.

ORDINAL PREFERENCES

- If person i strictly prefers item A to item B , we write:
 $A \succ_i B$.
- If person i weakly prefers item A to item B , we write:
 $A \succeq_i B$
- If person i is indifferent between item A to item B , we write: $A \sim_i B$
- We make 2 assumptions on preferences. Specifically,
 - that preferences are **complete** (each pair can be compared); that is, either $A \succeq_i B$ or $B \succeq_i A$ or both; and
 - that preferences are **transitive**; that is, if $A \succ_i B$ and $B \succ_i C$, then $A \succ_i C$.

PAYOFF FUNCTION

- When using ordinal preferences, we can assign a payoff function to the preferences.
- Example 1: if $A \succ_i B$, then, we could assign, for example,
 - $u(A) = 2$ and $u(B) = 1$.
 - In fact, any $u(A)$ and $u(B)$ such that $u(A) > u(B)$ would do.
- Example 2: if $A \succ_i B$ and $B \succ_i C$, then, we could assign, for example,
 - $u(A) = 3$, $u(B) = 2$ and $u(C) = 1$.
 - In fact, any $u(A)$, $u(B)$ and $u(C)$ such that $u(A) > u(B) > u(C)$ would do.
- Since preferences are ordinal, the payoff function does not convey intensity.

Strategic Games with Ordinal Preferences

Definition

A **strategic game with ordinal preferences** consists of:

- ① a set of **players**,
- ② a set of **actions** for each player, and
- ③ **preferences** over the set of action profiles for each player.

- An action profile is a list of specific actions for each player.
- The game does not contain time information, as it assumes players' moves are simultaneous.

NORMAL-FORM GAME TABLE

- A 2×2 game is represented with a game table as illustrated below.

Player 2

		Player 2	
		L	R
Player 1	U	a_1, a_2	b_1, b_2
	D	c_1, c_2	d_1, d_2

PRISONER'S DILEMMA

- The game was first posed by Flood and Dresher at RAND in 1950.
- The game consists of the following elements.
 - **Players:** There are two suspects.
 - **Actions:** Stay quiet or squeal.
 - **Preferences:**
 - Both squeal \rightarrow they each get 10 years in prison.
 - Both stay quiet \rightarrow they each get 2 years in prison.
 - One squeals, the other stays quiet \rightarrow the one that squeals gets 0 years, the other gets 15 years.

$$(S, SQ) \succ_i (SQ, SQ) \succ_i (S, S) \succ_i (SQ, S)$$

PRISONER'S DILEMMA (CONT.)

		Prisoner 2	
		Stay Quiet	Squeal
Prisoner 1	Stay Quiet	2,2	0,3
	Squeal	3,0	1,1

PRISONER'S DILEMMA (EXAMPLES)

		Firm 2	
		High Price	Low Price
Firm 1	High Price	300,300	0,400
	Low Price	400,0	200,200

		Athlete 2	
		Clean	Steroids
Athlete 1	Clean	5,5	2,8-c
	Steroids	8-c,2	5-c,5-c

Battle of the Sexes

- The game was first posed by Luce and Raiffa in 1957.
- The game consists of the following elements.
 - **Players:** There is a man and a woman.
 - **Actions:** Go to boxing or opera.
 - **Preferences:**
 - Meet at the boxing game \rightarrow man earns a payoff of 2 and woman of 1.
 - Meet at the opera \rightarrow woman earns a payoff of 2 and man of 1.
 - Don't meet each other \rightarrow they each get a payoff of 0.

$$(B, B) \succ_1 (O, O) \succ_1 (O, B) \sim_1 (B, O)$$

$$(O, O) \succ_2 (B, B) \succ_2 (O, B) \sim_2 (B, O)$$

Battle of the Sexes (Cont.)

		Player 2	
		Boxing	Opera
Player 1	Boxing	2,1	0,0
	Opera	0,0	1,2

BATTLE OF THE SEXES (EXAMPLES)

		Firm 2	
		Windows	OSX
Firm 1	Windows	20,20-c	10,10
	OSX	10,10	20-c,20

		Firm 2	
		LA	NY
Firm 1	LA	10-c,10	2,2
	NY	2,2	10,10-c

Chicken Game

- The game was first posed by biologist John Maynard Smith in 1973.
- The game consists of the following elements.
 - **Players:** There are two drivers.
 - **Actions:** Go straight or swerve.
 - **Preferences:**
 - If one goes straight and the other swerves \rightarrow the one that swerved is the chicken.
 - If both swerve \rightarrow at least they do not crash.
 - If both go straight \rightarrow they crash.

$$(S, Sw) \succ_i (Sw, Sw) \succ_i (Sw, S) \succ_i (S, S)$$

CHICKEN (CONT.)

Player 2

		Player 2	
		Swerve	Straight
Player 1	Swerve	3,3	2,4
	Straight	4,2	1,1

CHICKEN (EXAMPLES)

		US	
		Compromise	Escalate
USSR	Compromise	3,3	1,5-c
	Escalate	5-c,1	1-c,1-c

		Democrats	
		Raise Debt Ceiling	Keep Debt Ceiling
Republicans	Cut Spending	3,3	2,4
	Keep Current	4,2	1,1

Stag Hunt

- The game was first posed by philosopher Jean-Jacques Rousseau in 1775.
- The game consists of the following elements.
 - **Players:** There are two hunters.
 - **Actions:** Stag or Hare.
 - **Preferences:**
 - Hunt stag solo \rightarrow the individual gets 0 units of food.
 - Hunt hare solo \rightarrow the individual gets 1 unit of food.
 - Hunt stag with other player \rightarrow each gets 2 units of food.

$$(S, S) \succ_i (H, H) \sim_i (H, S) \succ_i (S, H)$$

STAG HUNT (CONT.)

Player 2

		Player 2	
		Stag	Hare
Player 1	Stag	2,2	0,1
	Hare	1,0	1,1

STAG HUNT (EXAMPLES)

		Worker 2	
		High Effort	Low Effort
Worker 1	High Effort	$4-c, 4-c$	$1-c, 1$
	Low Effort	$1, 1-c$	$1, 1$

		Depositor 2	
		Deposit	Withdraw
Depositor 1	Deposit	$3, 3$	$0, 1$
	Withdraw	$1, 0$	$1, 1$

MATCHING PENNIES

- The game was first posed by von Neumann (1928).
- The game consists of the following elements.
 - **Players:** There are two individuals.
 - **Actions:** Choose heads or tails.
 - **Preferences:**
 - Player 1 wins \rightarrow the actions match.
 - Player 2 wins \rightarrow the actions do not match.

$$(H, H) \sim_1 (T, T) \succ_1 (H, T) \sim_1 (T, H)$$

$$(H, T) \sim_2 (T, H) \succ_2 (H, H) \sim_2 (T, T)$$

MATCHING PENNIES (CONT.)

Player 2

		Player 2	
		Heads	Tails
Player 1	Heads	$1, -1$	$-1, 1$
	Tails	$-1, 1$	$1, -1$

MATCHING PENNIES (EXAMPLES)

		Goalie	
		East	West
Kicker	East	-1,1	1,-1
	West	1,-1	-1,1

		Driver	
		Speed	Obey
Policeman	Check	1,-1	-1,1
	Sleep	-1,1	1,-1

NASH EQUILIBRIUM

- An equilibrium is a state in which opposing forces or influences are balanced.
- If a is an action profile, $a = (a_1, a_2, \dots, a_n)$, then a_{-i} is an action profile containing everyone's action except player i , i.e., $a_{-i} = (a_1, a_2, \dots, a_{i-1}, a_{i+1}, \dots, a_n)$.

Definition

The action profile a^* in a strategic game with ordinal preferences is a **Nash equilibrium** (NE) if for every player i ,

$$u_i(a^*) \geq u_i(a_i, a_{-i}^*) \text{ for every action profile } a_i \text{ of player } i,$$

where u_i is a payoff function that represents player i 's preferences.

BEST RESPONSE

- The best response for player i given action(s) a_{-i} is written as:

$$B_i(a_{-i}) = \{a_i \text{ in } A_i : u_i(a_i, a_{-i}) \geq u_i(a'_i, a_{-i}) \text{ for all } a'_i \text{ in } A_i\}.$$

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	L	R
U	2,0	3,3
D	2,5	1,4

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$$BR_1(L) = \{U, D\}$$

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	L	R
U	2,0	3,3
D	2,5	1,4

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$$BR_2(U) = \{R\}$$

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	L	R
U	2,0	3,3
D	2,5	1,4

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$$BR_2(D) = \{L\}$$

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	L	R
U	<u>2</u> , 0	3, 3
D	<u>2</u> , 5	1, 4

$$BR_1(L) = \{U, D\}$$

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	L	R
U	<u>2</u> , 0	<u>3</u> , 3
D	<u>2</u> , 5	1, <u>4</u>

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	L	R
U	<u>2</u> , 0	<u>3</u> , <u>3</u>
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	L	R
U	<u>2</u> , 0	<u>3</u> , <u>3</u>
D	<u>2</u> , <u>5</u>	1, <u>4</u>

$$BR_1(L) = \{U, D\}$$

$$BR_1(R) = \{U\}$$

$$BR_2(U) = \{R\}$$

$$BR_2(D) = \{L\}$$

ALTERNATIVE DEFINITION OF A NASH EQUILIBRIUM

Proposition

The action profile a^ is a **Nash equilibrium** of a strategic game with ordinal preferences if and only if every player's action is a best response to the other players' actions; that is,*

$$a_i^* \in B_i(a_{-i}^*) \text{ for every player } i.$$

- An action profile is a Nash equilibrium if every player's action is best responding to each other.

NASH EQUILIBRIUM (EXAMPLE)

- Consider the following game consisting of the following elements.
 - **Players:** $\{1, 2, 3, 4, 5, 6, 7\}$
 - **Actions:** $\{A, B, C, D\}$
 - **Payoffs:** represented with u_i .

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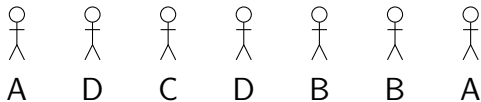
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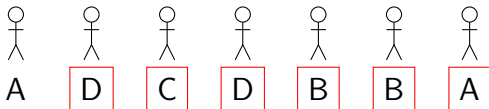
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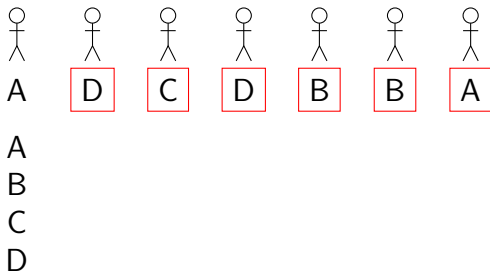
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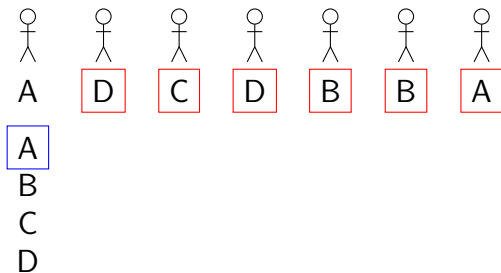
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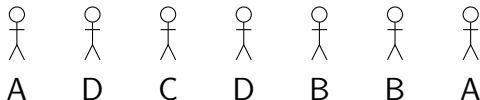
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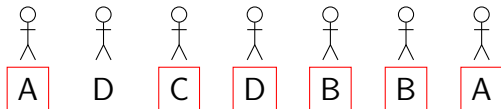
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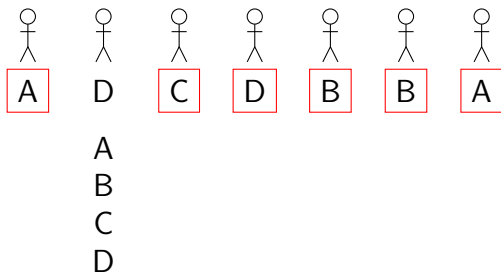
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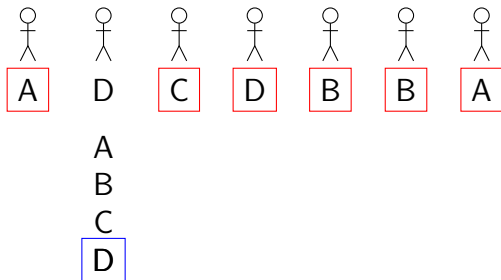
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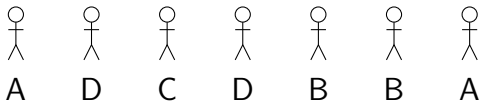
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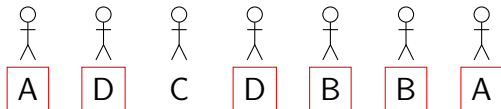
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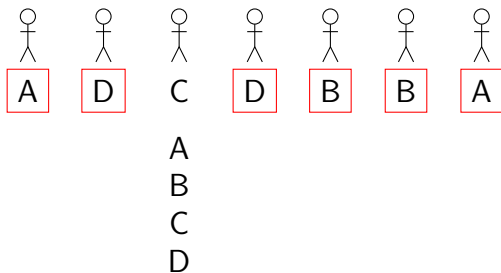
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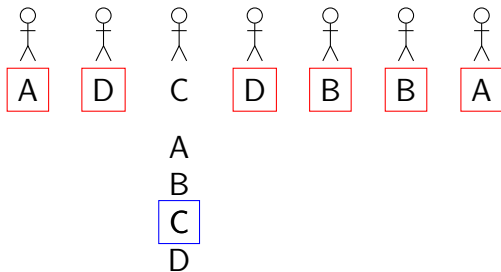
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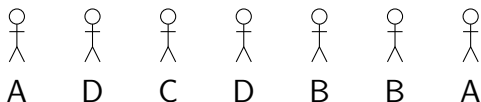
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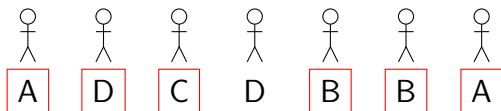
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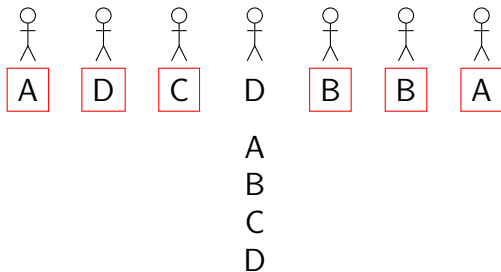
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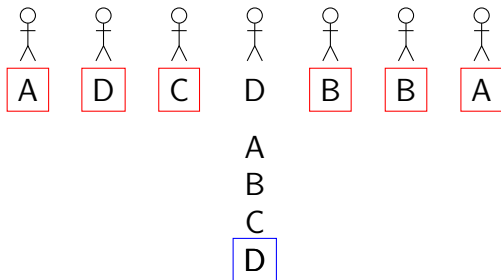
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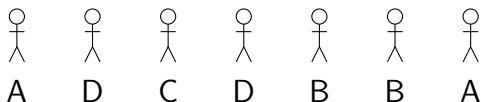
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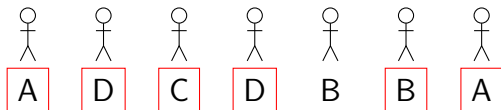
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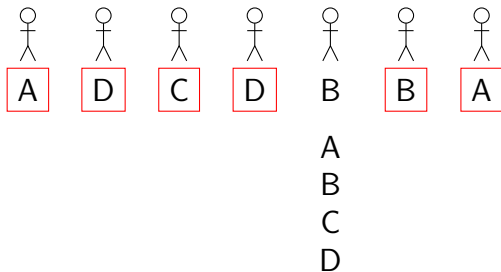
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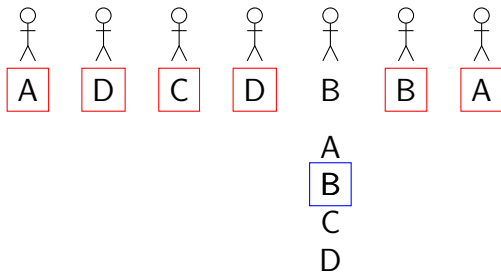
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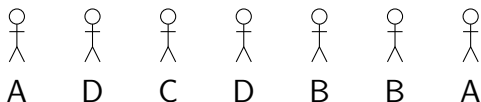
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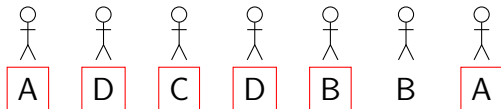
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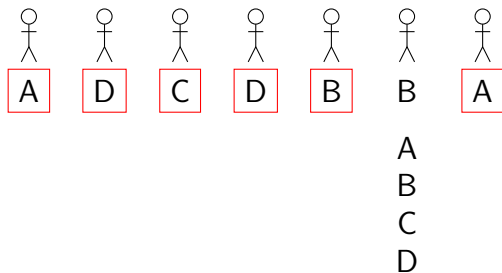
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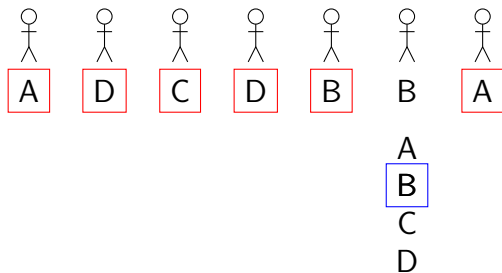
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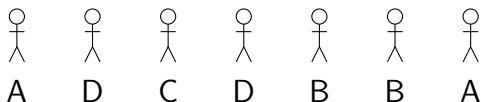
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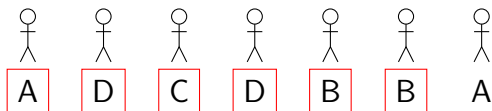
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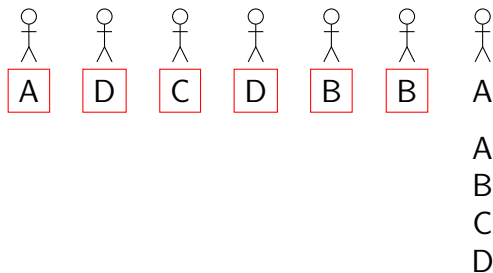
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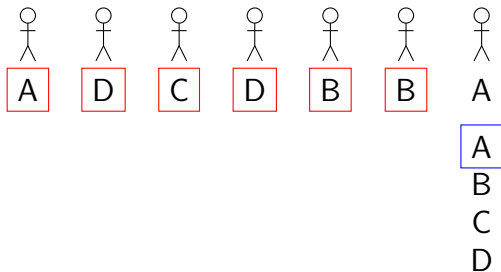
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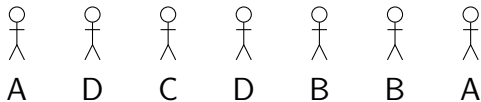
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It is in no player's interest to unilaterally deviate from a Nash Equilibrium.

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	A	0,0	3,4

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		Player 2	
		C	D
Player 1	B	4,4	2,5 *
	A	5,2 *	0,0

(c) Chicken

		Player 2	
		C	D
Player 1	B	4,3 *	0,0
	A	0,0	3,4 *

(d) Battle of the Sexes

		Player 2	
		H	T
Player 1	H	4,0	0,4
	T	0,4	4,0

(e) Matching Pennies

HOW TO FIND THE NASH EQUILIBRIUM?

Find all Nash Equilibria in the following games.

		Player 2	
		C	D
Player 1	B	2,2	0,3
	A	3,0	1,1 *

(a) Prisoner's Dilemma

		Player 2	
		C	D
Player 1	B	4,4 *	1,3
	A	3,1	3,3 *

(b) Stag Hunt

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Player 1	B	4,4	2,5 *
	A	5,2 *	0,0

(c) Chicken

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		C	D
Player 1	B	4,3 *	0,0
	A	0,0	3,4 *

(d) Battle of the Sexes

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Player 1	H	4,0	0,4
	T	0,4	4,0

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Strictly Dominated Strategy

Definition

In a SGWOP, player i 's action a_i'' , strictly dominates her actions a_i' , if $u_i(a_i'', a_{-i}) > u_i(a_i', a_{-i})$ for every list a_{-i} of the other players' actions, where u_i is player i 's payoff function. We say that the action a_i' is **strictly dominated**.

	L	R
U	3, 3	1, 1
D	4, 1	2, 2

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U	3, <u>3</u>	1, 1
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In a SGWOP, player i 's action a_i'' , strictly dominates her actions a_i' , if $u_i(a_i'', a_{-i}) > u_i(a_i', a_{-i})$ for every list a_{-i} of the other players' actions, where u_i is player i 's payoff function. We say that the action a_i' is **strictly dominated**.

	L	R
U	3, <u>3</u>	1, 1
D	<u>4</u> , 1	<u>2</u> , <u>2</u>

- U is strictly dominated by D.

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In a SGWOP, player i 's action a_i'' , strictly dominates her actions a_i' , if $u_i(a_i'', a_{-i}) > u_i(a_i', a_{-i})$ for every list a_{-i} of the other players' actions, where u_i is player i 's payoff function. We say that the action a_i' is **strictly dominated**.

	L	R
U	3, <u>3</u>	1, 1
D	<u>4</u> , 1	<u>2</u> , <u>2</u>

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In a SGWOP, player i 's action a_i'' , strictly dominates her actions a_i' , if $u_i(a_i'', a_{-i}) > u_i(a_i', a_{-i})$ for every list a_{-i} of the other players' actions, where u_i is player i 's payoff function. We say that the action a_i' is **strictly dominated**.

	L	R
U	3, <u>3</u>	1, 1
D	<u>4</u> , 1	<u>2</u> , <u>2</u>

- U is strictly dominated by D.
- Neither L nor R are strictly dominated.

Strictly Dominated Strategy

Definition

In a SGWOP, player i 's action a_i'' , strictly dominates her actions a_i' , if $u_i(a_i'', a_{-i}) > u_i(a_i', a_{-i})$ for every list a_{-i} of the other players' actions, where u_i is player i 's payoff function. We say that the action a_i' is **strictly dominated**.

	L	R
U	3, <u>3</u>	1, 1
D	<u>4</u> , 1	<u>2</u> , <u>2</u>

- U is strictly dominated by D.
- Neither L nor R are strictly dominated.
- A strictly dominated strategy will never be played in a Nash equilibrium.

WEAKLY DOMINATED STRATEGY

Definition

In a SGWOP, player i 's action a''_i , weakly dominates her actions a'_i , if $u_i(a''_i, a_{-i}) \geq u_i(a'_i, a_{-i})$ for every list a_{-i} of the other players' actions, and,

$u_i(a''_i, a_{-i}) > u_i(a'_i, a_{-i})$ for at least one list a_{-i} of the other players' actions,

where u_i is player i 's payoff function. We say that the action a'_i is **weakly dominated**.

EXAMPLE

	A	B	C
Z	3, 4	6, 3	5, 2
Y	3, 2	5, 1	2, 3
X	2, 3	2, 2	2, 1

Find all:

- (i) weakly dominated strategies,
- (ii) strictly dominated strategies,
- (iii) Nash Equilibria.

STRICT NASH EQUILIBRIUM

Definition

The action profile a^* in a SGWOP is a **strict Nash equilibrium**, if for every player i ,

$$u_i(a^*) > u_i(a_i, a_{-i}^*) \text{ for every action profile } a_i \text{ of player } i,$$

where u_i is a payoff function that represents player i 's preferences.

STRICT NASH EQUILIBRIUM (EXAMPLE)

	L	R
D	0, 0	2, 1
D	3, 2	0, 2

- The game has 2 Nash equilibria.
- Only 1 Nash equilibrium is strict.
- A Nash equilibrium might consist of weakly dominated strategies.
- The non-strict Nash equilibrium is less stable.

STRICT NASH EQUILIBRIUM (EXAMPLE)

	L	R
D	0, 0	2, 1
D	3, 2	0, 2

- The game has 2 Nash equilibria.
- Only 1 Nash equilibrium is strict.
- A Nash equilibrium might consist of weakly dominated strategies.
- The non-strict Nash equilibrium is less stable.

STRICT NASH EQUILIBRIUM (EXAMPLE)

	L	R
D	0, 0	2, 1
D	3, 2	0, 2

- The game has 2 Nash equilibria.
- Only 1 Nash equilibrium is strict.
- A Nash equilibrium might consist of weakly dominated strategies.
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STRICT NASH EQUILIBRIUM (EXAMPLE)

	L	R
D	0, 0	2, 1
D	<u>3</u> , 2	0, 2

- The game has 2 Nash equilibria.
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STRICT NASH EQUILIBRIUM (EXAMPLE)

	L	R
D	0, 0	<u>2</u> , 1
D	<u>3</u> , 2	0, 2

- The game has 2 Nash equilibria.
- Only 1 Nash equilibrium is strict.
- A Nash equilibrium might consist of weakly dominated strategies.
- The non-strict Nash equilibrium is less stable.

STRICT NASH EQUILIBRIUM (EXAMPLE)

	L	R
U	0, 0	<u>2</u> , <u>1</u>
D	<u>3</u> , 2	0, 2

- The game has 2 Nash equilibria.
- Only 1 Nash equilibrium is strict.
- A Nash equilibrium might consist of weakly dominated strategies.
- The non-strict Nash equilibrium is less stable.

STRICT NASH EQUILIBRIUM (EXAMPLE)

	L	R
U	0, 0	<u>2</u> , <u>1</u>
D	<u>3</u> , <u>2</u>	0, <u>2</u>

- The game has 2 Nash equilibria.
- Only 1 Nash equilibrium is strict.
- A Nash equilibrium might consist of weakly dominated strategies.
- The non-strict Nash equilibrium is less stable.

SYMMETRIC GAMES

Definition

A two-player SGWOP is **symmetric** if the players' set of actions are the same and the players' preferences are represented by payoff function u_1 and u_2 for which $u_1(a_1, a_2) = u_2(a_2, a_1)$ for every action pair (a_1, a_2) .

- Players are all homogeneous and no roles are assigned.

Definition

An action profile a^* in a symmetric SGWOP is a **symmetric Nash equilibrium** if it is a Nash equilibrium and a_i^* is the same for every player i .

EXAMPLE

	A	B	C
Z	1, 1	2, 1	4, 1
Y	1, 2	5, 5	3, 6
X	1, 4	6, 3	0, 0

Find all:

(i) Nash Equilibria,

(ii) symmetric Nash Equilibria.